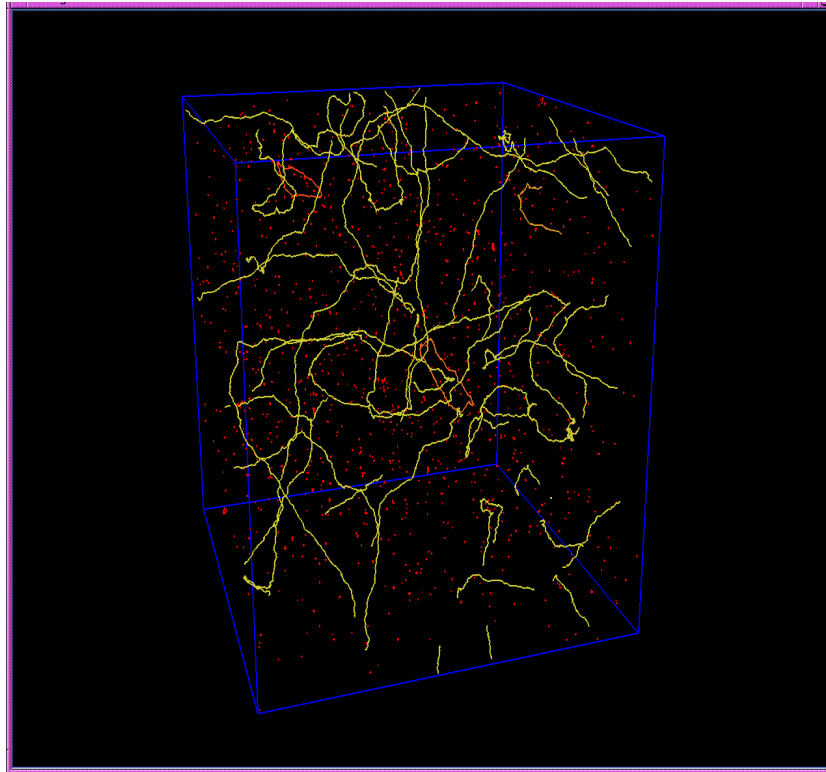


FUTURE OPPORTUNITIES FOR THE DETECTION OF TOPOLOGICAL DEFECTS



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STRINGS IN THE ABELIAN-HIGGS MODEL

LAGRANGIAN :
$$\mathcal{L} = |D_\mu \Phi|^2 - \frac{1}{4} F_{\mu\nu} F^{\mu\nu} - \frac{1}{4} \lambda (|\Phi|^2 - \eta^2)^2$$

VORTEX FIELD CONFIGURATION

$$\Phi(r, \theta) = f(r) \exp[in\theta]$$

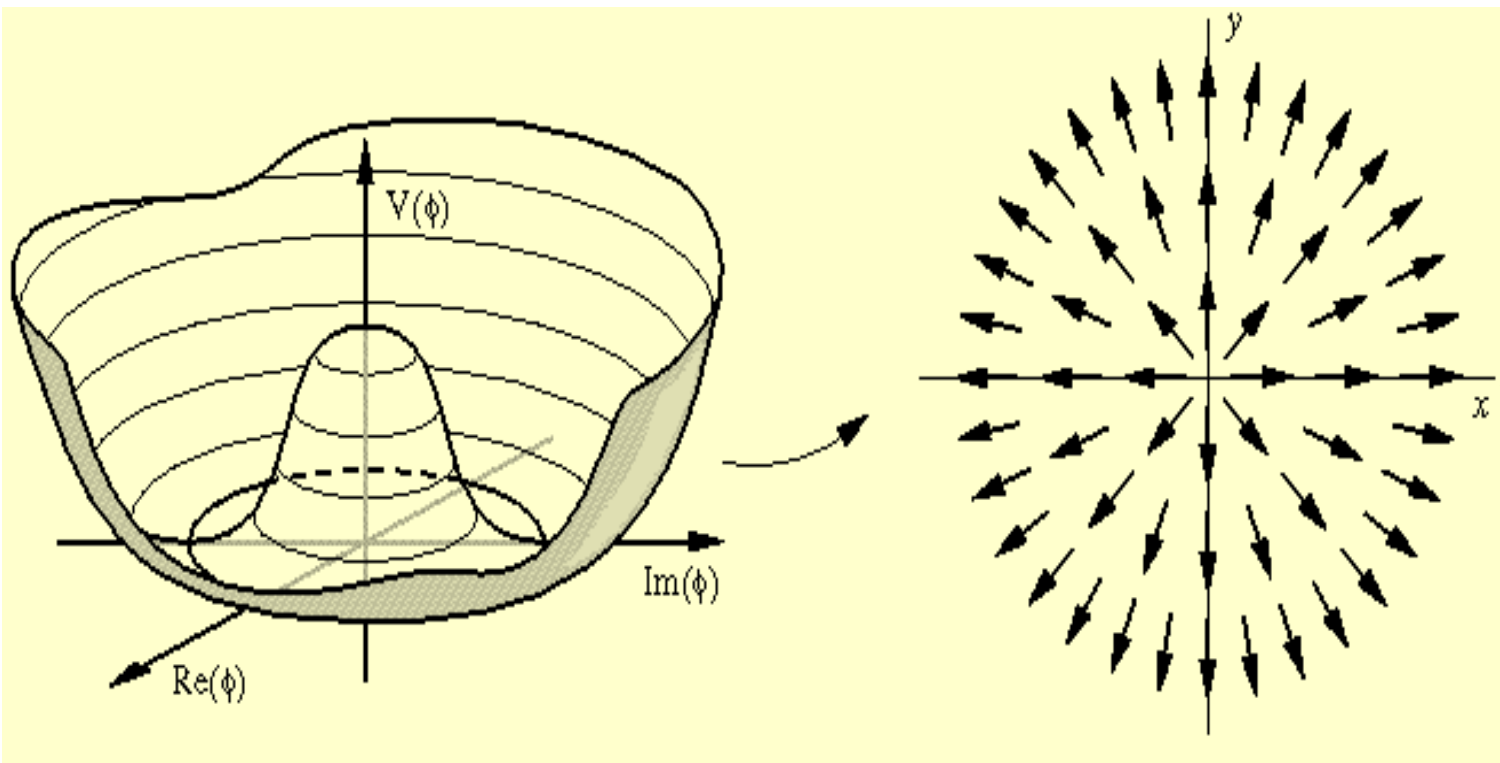
$$A_\theta(r) = \frac{n\alpha(r)}{er}$$

MASS / UNIT LENGTH

$$G\mu \approx \left(\frac{\eta}{M_{\text{pl}}} \right)^2$$

CORE WIDTH

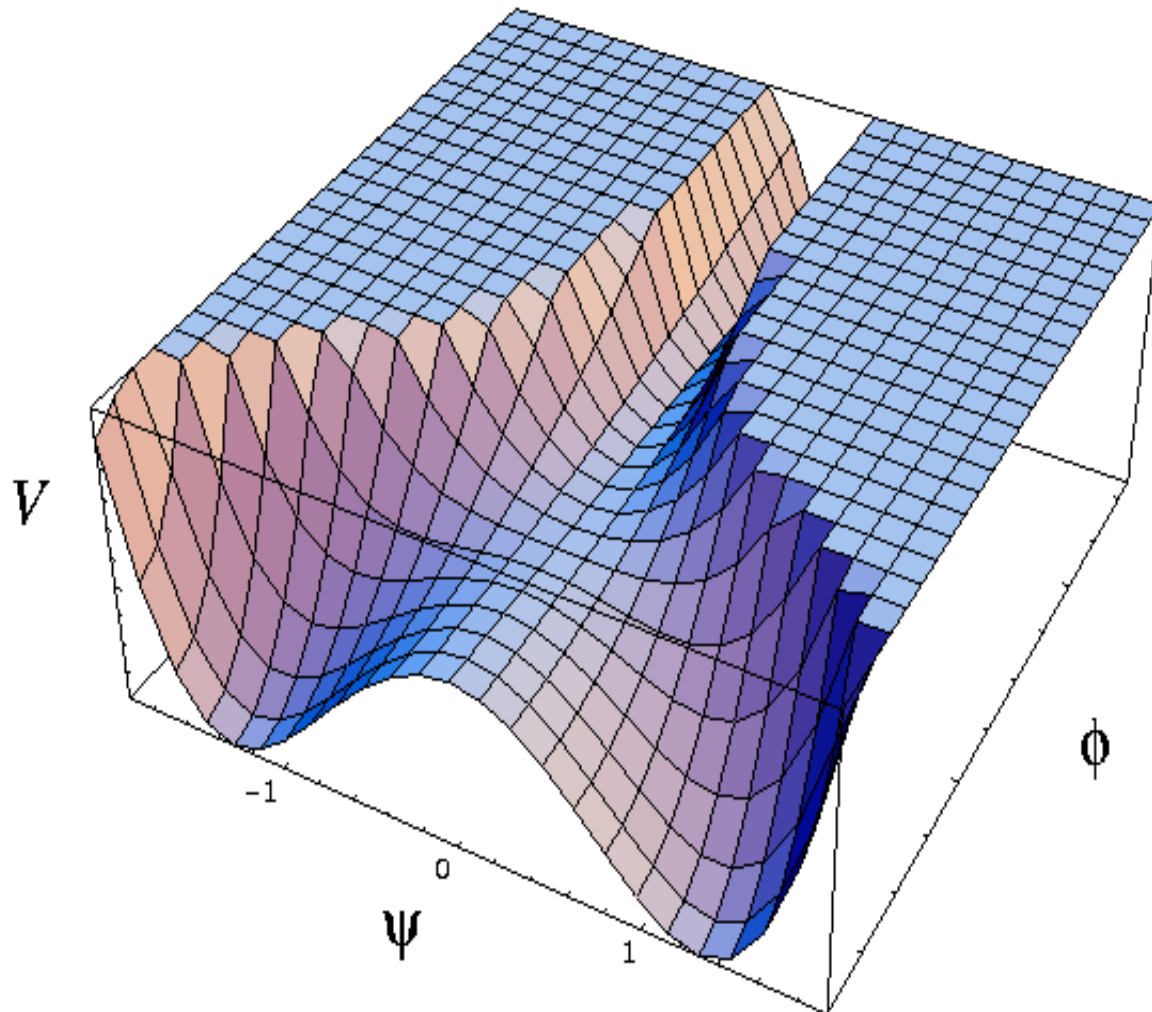
$$\Delta \sim \eta^{-1}$$



VORTEX FIELD
CONFIGURATION

HYBRID INFLATION

$$V(\phi, \psi) = \frac{1}{2}m^2\phi^2 + \frac{\lambda}{4}(|\psi|^2 - \eta^2)^2 + \frac{1}{2}g\phi^2|\psi|^2$$



INFLATON DIRECTION
DESTABILIZED AT

$$\phi_c = \sqrt{\frac{\lambda\eta^2}{g}}$$

$$\phi > \phi_c \quad \rightarrow \quad m_{\psi}^2 > 0$$

$$\phi < \phi_c \quad \rightarrow \quad m_{\psi}^2 < 0$$



PHASE TRANSITION
& FORMATION OF STRINGS

A FEW NUMBERS !

$$\frac{\Delta T}{T} \sim \frac{\Delta \rho}{\rho} \sim 8\pi G\mu \sim 10^{-5} \quad \text{for a GUT scale phase transition}$$

Models which produce topological defects are constrained to have low, possibly undetectable inflation generated B-modes

Consider a potential : $V(\phi) = V_0 F(\phi/M_{\text{pl}})$

Typically, one finds $\frac{G\mu}{c^2} = 2\pi a \left(\frac{V_0}{M_{\text{pl}}}\right)^{1/2}$ a is model dependent

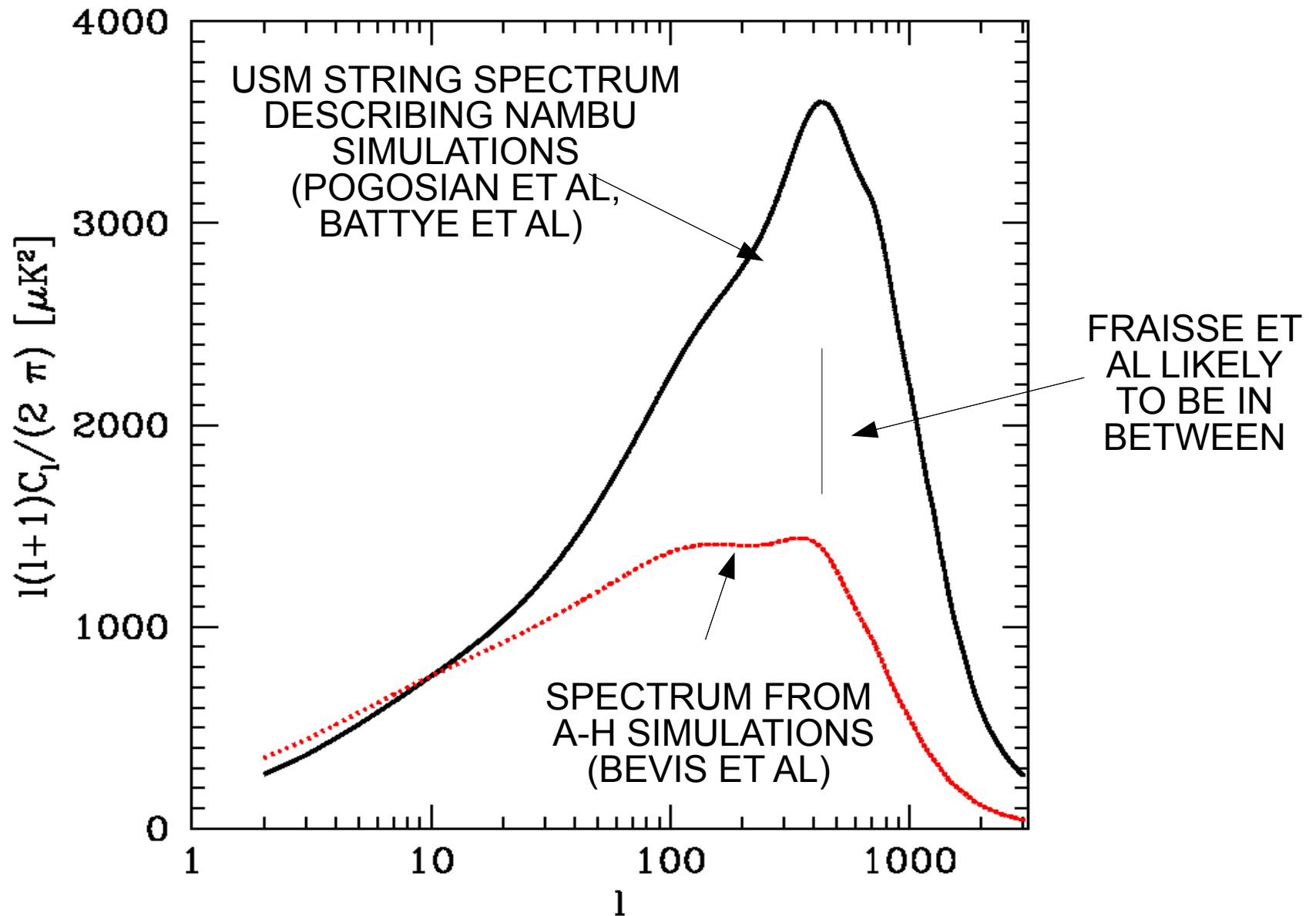
$$\longrightarrow \mathcal{P}_T \propto \left(\frac{G\mu/c^2}{a}\right)^2 F(\phi/M_{\text{pl}}) \quad \& \quad r < 10^{-3} \frac{F}{a^2}$$

Examples : $F(x) = 1 - \frac{\gamma}{x^4}$, $F(x) = A + B \log x$, $F(x) = 1 + Ax^p$
 Brane inflation SUSY hybrid inflation

WAYS TO DETECT COSMIC STRINGS

- Temperature power spectrum
 - strongest present limit which will be improved by Planck
- Direct detection of the Kaiser-Stebbins effect
 - line-like discontinuities
 - non-Gaussianity
- B-modes
 - defect models naturally produce vector and tensor modes
- Pulsar timing / Gravitational lensing etc
 - no relevant to the discussion here

2 POSSIBLE STRING SPECTRA

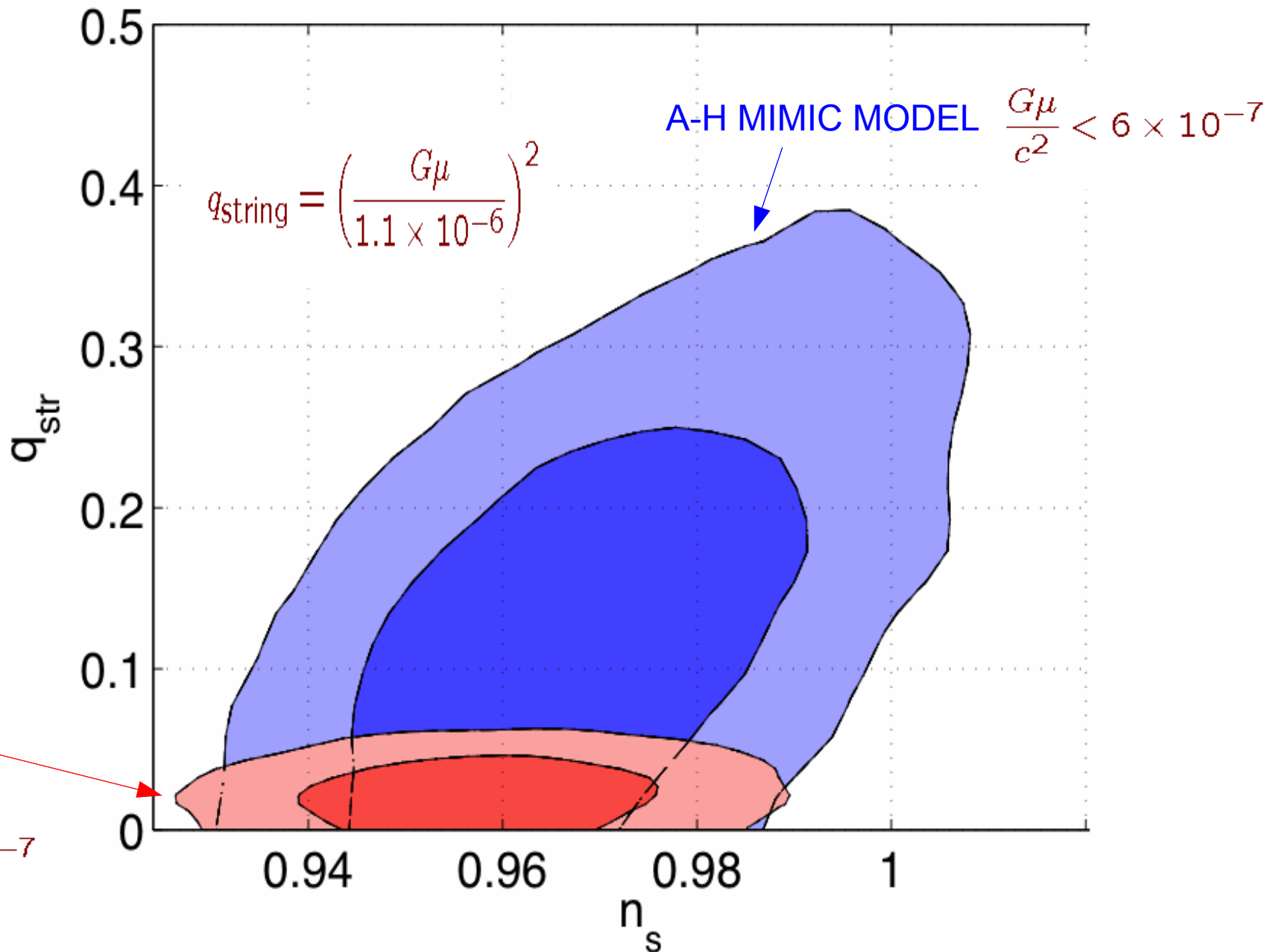


NEITHER LOOK LIKE THE WMAP DATA – CONSTRAIN A SUBDOMINANT COMPONENT !

UP TO DATE CONSTRAINTS

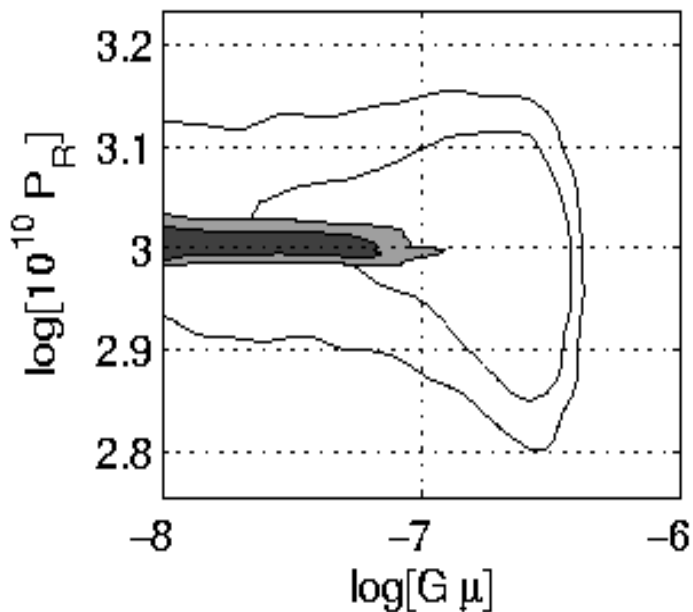
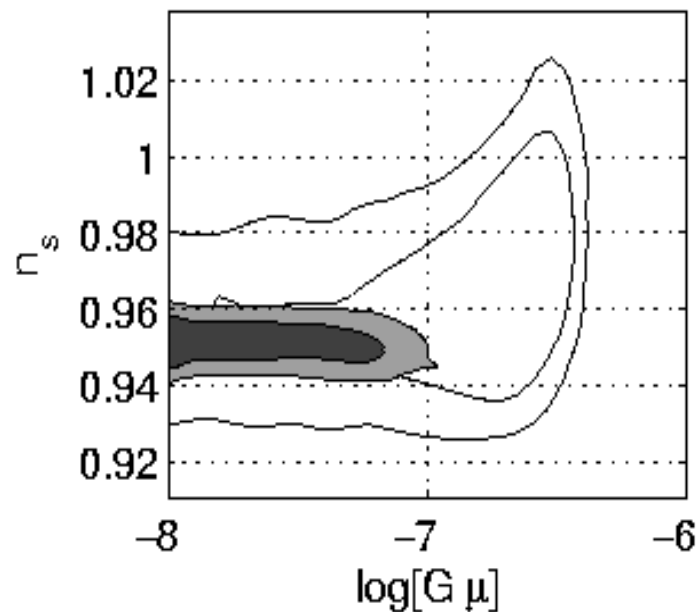
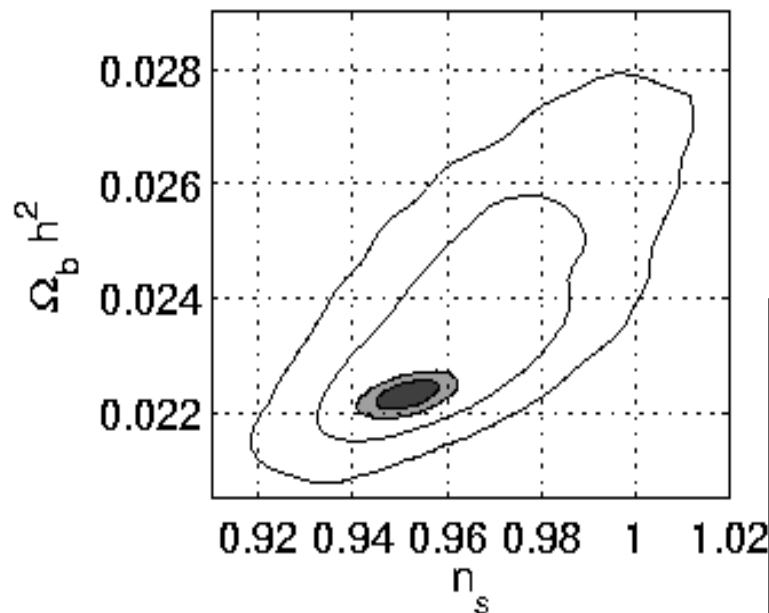
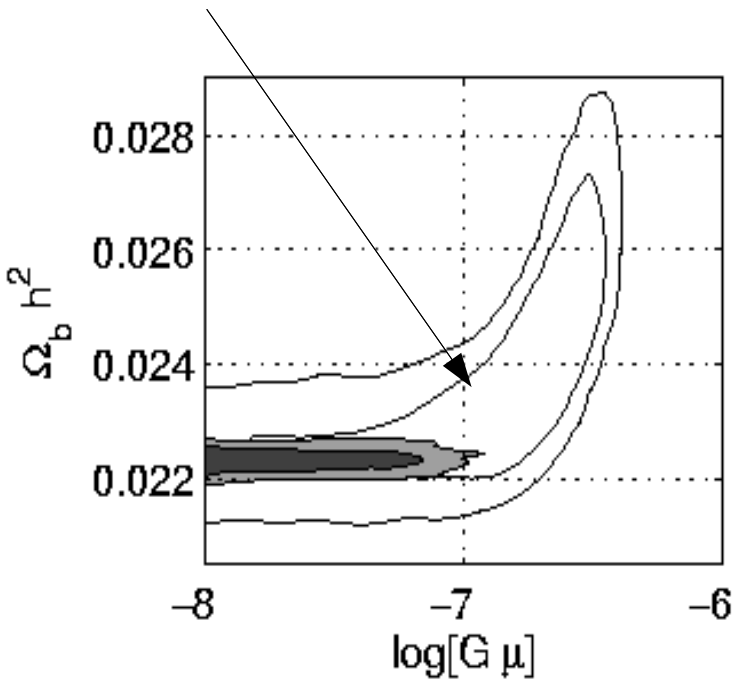
(Battye & Moss, 2010)

BASED ON CMB (WMAP5+OTHERS) + SDSS (TEGMARK ET AL) + BBN (PETTINI ET AL)



SIMULATED PLANCK DATA

(Battye, Garbrecht,
Moss, Stoica, 2008)



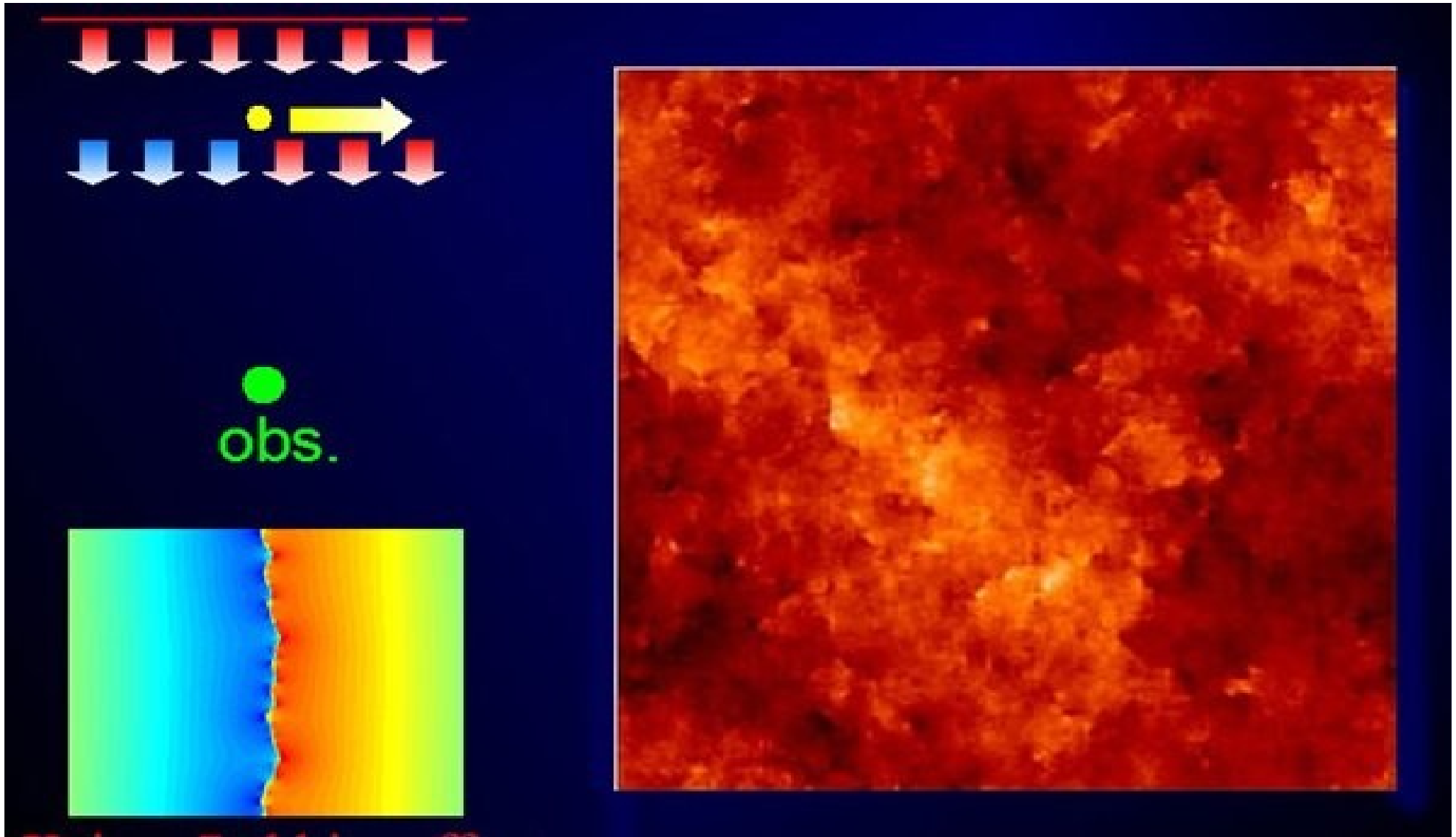
Projected
constraint

$$\frac{G\mu}{c^2} < 7 \times 10^{-8}$$

based on
TT, TE & EE

DIRECT DETECTION & NON-GAUSSIANITY

KAISER-STEBBINS EFFECT

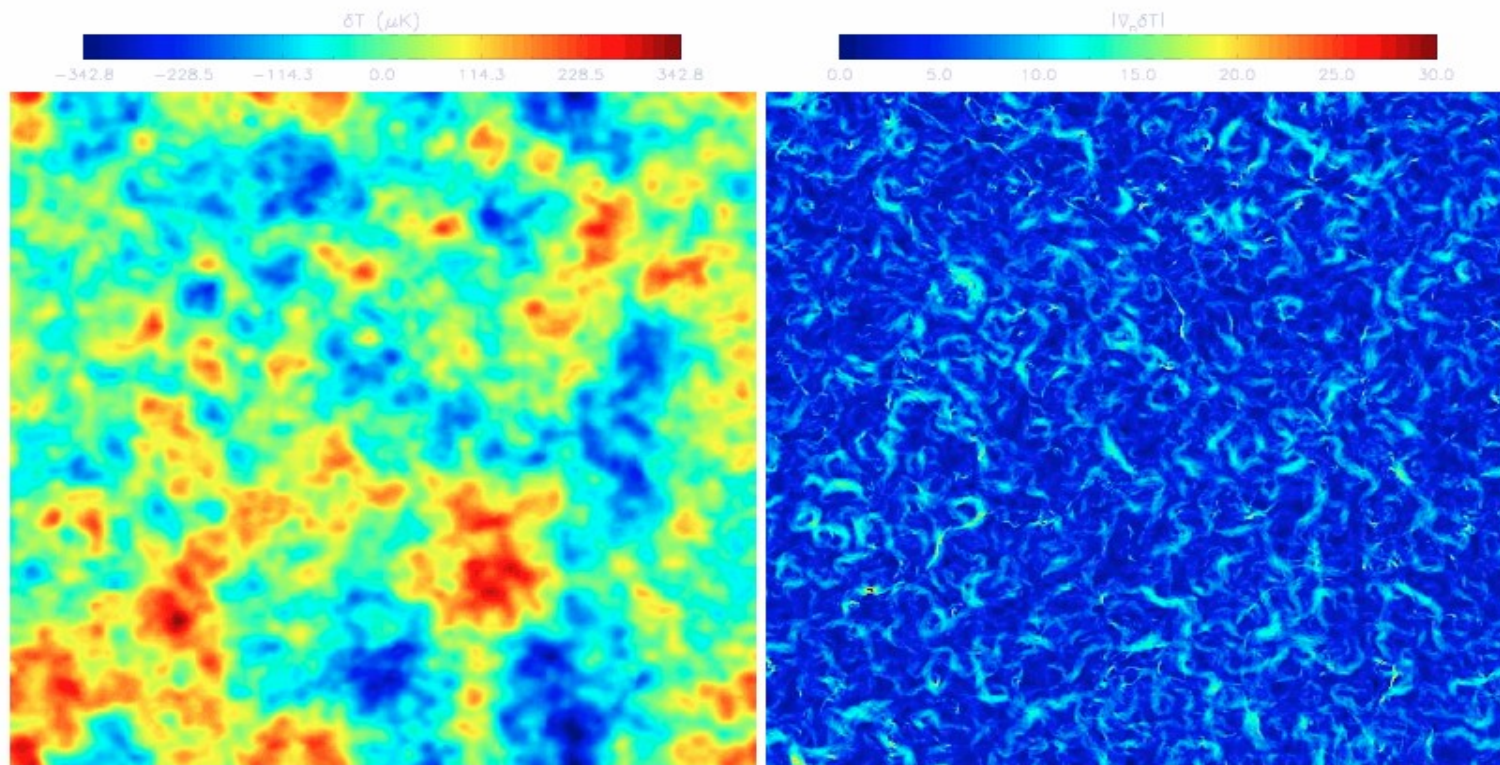


CMB
ANISOTROPY :

$$\frac{\Delta T}{T} = 8\pi G\mu\gamma v$$

(Bennett, Bouchet.
Stebbins)

RECENT WORK



(Fraisse, Ringeval,
Spegel & Bouchet,
2008)

Temperature

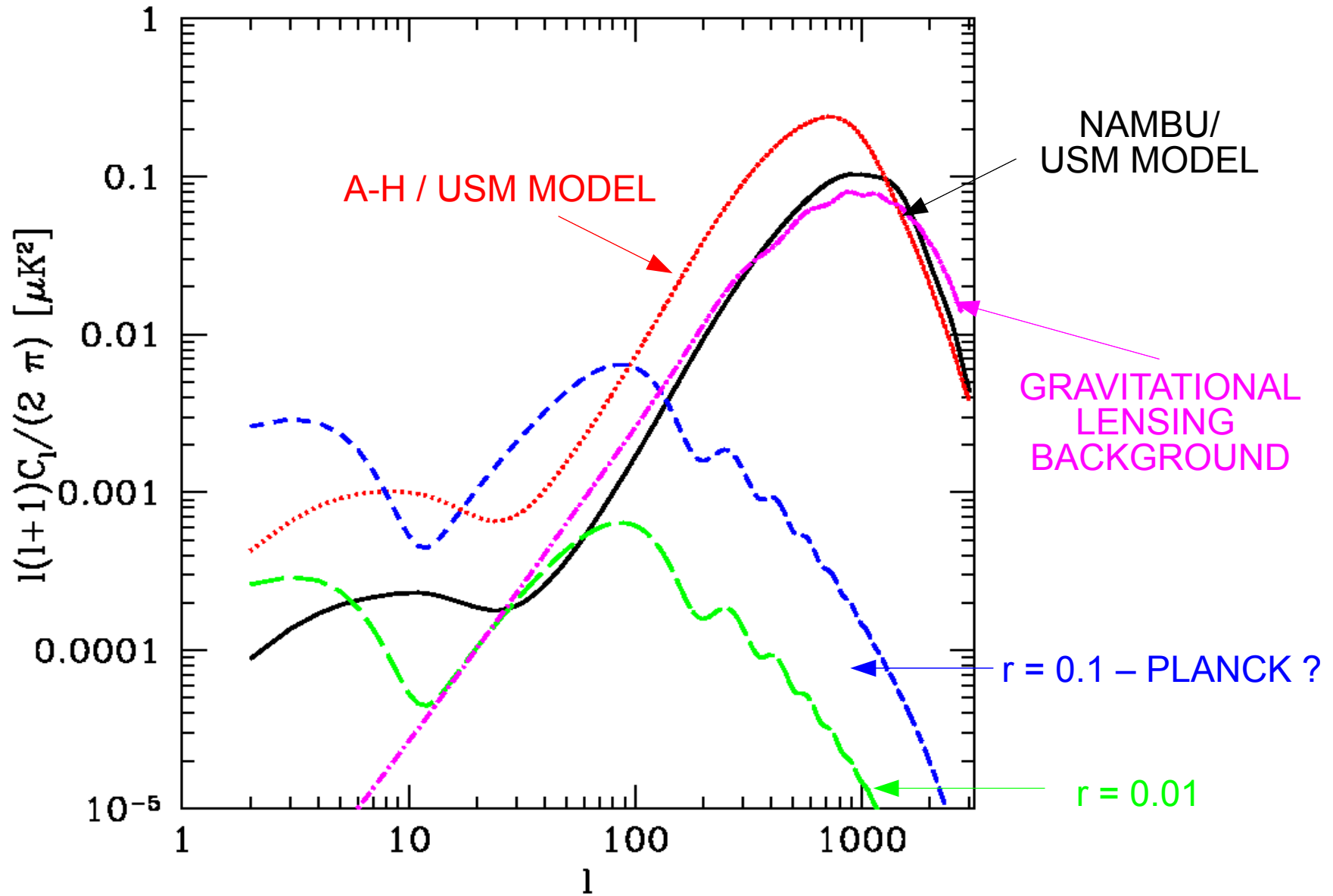
Temperature gradient

Also Bispectrum and Trispectrum :

- Hindmarsh, Ringeval & Suyama
- Regan & Shellard

→ sensitivity & resolution

B-MODE POLARIZATION



Limit from present data (eg QuAD) $\longrightarrow \frac{G\mu}{c^2} < 5.5 \times 10^{-7}$

SUMMARY & CONCLUSIONS

- Present CMB constraint:

$$\frac{G\mu}{c^2} < 2.5 \times 10^{-7} \quad (\text{NAMBU SIMULATIONS}) \quad \frac{G\mu}{c^2} < 6 \times 10^{-7} \quad (\text{ABELIAN-HIGGS SIMULATIONS})$$

- about factor of 4 improvement expected from Planck
- Direct detection & non-Gaussianity
 - requires high resolution
 - improvements beyond Planck possible (Wandelt Talk)
- B-modes
 - Models with strings \rightarrow low r
 - Defect models produce B-modes via vectors
 - Nambu case difficult due to potential confusion with lensing